

**Problem 1 (Basic Monopoly)**

Consider a monopolist with total cost  $TC = \frac{1}{2}y^2$  facing a demand  $p(y) = 300 - y$ .

- a) What is the profit maximizing level of output and the resulting price?
  
  
  
  
  
  
  
  
  
  
- b) What is the producer surplus (PS) at this level of output?
- c) What is the consumer surplus (CS) at this level of output?
- d) Is the outcome Pareto efficient? If not, what is the deadweight loss (DWL)?

**Problem 2 (Monopoly and Price Discrimination)**

Airline BestFly is a monopolist in the market of Island Zee. It has to decide how many tickets,  $y$ , are to be sold for the next holiday season. The fixed cost of running the airline is  $F = \$40,000$  and the variable cost is given by  $C(y) = 100y$ . BestFly faces an inverse demand curve  $p(y) = 600 - y$ .

- a) Suppose BestFly can perfectly discriminate (first degree price discriminate). Calculate BestFly profits.

There are two types of travelers on the Island of Zee: business travelers with demand  $p^B = 1200 - 4y^B$  and tourist travelers with demand  $p^T = 400 - \frac{4}{3}y^T$ .

- b) Show that if BestFly does not discriminate, the aggregate inverse demand is the same as in part a).

- c) Find the level of sales, prices, profits, and demand elasticities' of each of the market segments (business and tourist travelers) under third degree price discrimination.
- d) Compare the PS and CS in the following three case: (1) uniform price (nondiscriminating monopolist), (2) perfect (first degree) price discrimination, and (3) third degree price discrimination.

**Problem 3 (Demand Elasticity)**

Suppose a monopolistic firm is facing the following demand:  $y(p) = 2 - p$ .

- a) Calculate the value of the demand elasticity  $\epsilon$  for  $y = 0$ ,  $y = 1$ , and  $y = 2$ .
- b) Write down the marginal revenue (MR) in terms of elasticity  $\epsilon$  and price  $p$ . What is the value of  $\epsilon$  when  $MR = 0$ ? What about when  $MR > 0$ ?
- c) Find the markup over the marginal cost (MC).